## CS480

# Bottom Up Parsing <br> Ch 4 p 195-215 + handouts! <br> Read chap 4 by Monday. 

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CS 480 - Spring 2013
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## The Plan

I hate wordy slides.
This topic is too precise for me to get correct without lots of hints.

- Bottom Up Parsing
- Handles
- Shift/Reduce
- Operator Precedence Parsing
- Building Operator Precedence Tables
- Wednesday: Build an OPT in class


## Bottom Up Parsing

- Build parse tree from leaves and work up!
- Reduce a string, w, to the start symbol, S
- Reduction: replace a substring that matches the RHS of a production with the LHS of that production
- Right most derivation is run in reverse.

```
S -> aABe
A -> Abc | b
B -> d
abbcde

\section*{Algorithm}
1) Look for a substring in \(w\) that matches the right side of any production.
2) Repeat step 1) with the new string \(w^{\prime}\) until the start symbol S is produced (accept) or we run out of matching possibilities (reject)
abbcde
- Problems?
\[
\begin{array}{lll}
S \rightarrow> & \text { aABe } \\
\text { A } \rightarrow \text { Abc | b } \\
\text { B } \rightarrow> & \text { d }
\end{array}
\]

\section*{Handle}
\[
\begin{aligned}
& S->\text { aABe } \\
& A->\text { Abc | b } \\
& \text { B } \rightarrow>\text { d }
\end{aligned}
\]
- A handle is a substring of a string that matches some production's right side such that a reduction to a nonterminal on the left can be done in one step along the reverse of a rightmost derivation.
abbcde

\section*{Practice}
- page 196/198
\[
\begin{aligned}
& E \rightarrow P E+E \\
& E \rightarrow> \\
& E \rightarrow \\
& E \rightarrow \\
& E \rightarrow> \\
& \text { id }
\end{aligned}
\]

Right Most Derivation
- Remember, we are doing bottom up parsing, so we start right here
\[
\begin{aligned}
E & \Rightarrow E+E \\
& \Rightarrow E+E \quad * E \\
& \Rightarrow E+E \quad * i d_{3} \\
& \Rightarrow E+i d_{2} * i d_{3} \\
& \Rightarrow i d_{1}+i d_{2} * i d_{3}
\end{aligned}
\]
- Ambiguous grammar so \(1+\quad={ }_{\text {rm }}\)
- Handle Pruning

\section*{How to choose a Handle}
- Add a restriction

We'll see an implementable algorithm for this later.
- Defn[Aho]: "A handle of a right-sentential form \(\gamma\) is a production \(A->\beta\) and a position of \(\gamma\) where the string \(\beta\) may be found and replaced by A to produce the previous rightsentential form in the rightmost derivation of \(\gamma\).
That is, if \(S=>^{*}{ }_{\mathrm{rm}} \alpha \mathrm{Aw}=>_{\mathrm{rm}} \alpha \beta \mathrm{w}\),
then \(\mathrm{A}->\beta\) in the position following \(\alpha\) is a handle of \(\alpha \beta \mathrm{w}\)."
\begin{tabular}{|c|c|c|}
\hline \multicolumn{2}{|l|}{\begin{tabular}{l}
Shift Re \\
- p199 ex4.24
\end{tabular}} & \[
\operatorname{ing} \left\lvert\, \begin{array}{lllll}
E & -> & E & + & E \\
E & -> & E & * & E \\
E & -> & ( & E & ) \\
E & -> & \text { id } &
\end{array}\right.
\] \\
\hline Stack & Input & Action \\
\hline \$ & id + id * id \$ & shift \\
\hline \$id & + id * id \$ & Reduce E -> id \\
\hline \$E & + id * id \$ & shift \\
\hline & & \\
\hline & & \\
\hline & & \\
\hline & & \\
\hline
\end{tabular}

\section*{CONFLICTS!}
- p 201 stmt -> if expr then stmt | if expr then stmt else stmt other
- Some CFGs have unresolvable conflicts
- shift/reduce
- reduce/reduce

Stack
Input
Action
\$ ... if expr then stmt else ... \$
?????

\section*{Operator Precedence Parsing}
- Form of Shift/Reduce parsing

This allows us to find handles!
- Two important properties for these shiftreduce parsers is that \(\boldsymbol{\varepsilon}\) does not appear on the right side of any production and no production has two adjacent nonterminals.
\[
\begin{aligned}
& E->E+E \\
& T->+T E T
\end{aligned}
\]

\section*{Precedence}
- We need to define three different precedence relations between pairs of terminals

\author{
Relation \\ Meaning \\ a <. b a yields precedence to b \\ \(a=. \quad b \quad a\) has the same precedence as b \\ \(a>. b\) \\ a takes precedence over b \\ They look like >, <, and == but are very different
}

\section*{Why?}
- Identify each handle using the precedence rules and reduce the right-sentential string, based on the precedence relations, to a start (accept) state.

\section*{Precedence Table}

Define precedence relations between terminals.
```

E -> E + T | T
T -> T * F | F
F -> id

```


\section*{How does this work? (high level) p205} \$ id + id * id \$
\$ <. id >. + <. id >. * <. id >. \$
- Scan from left (to right) until the first >. is found
- Then, scan backwards (left) until a \(<\). is found
- The handle is everything to the left of the \(>\). and right of the \(<\).
- Including surrounding nonterminals

\section*{In Code, p206 Algo 4.5}
- How to find a handle
- Use a stack
- If the precedence relation \(<\). or \(=\). holds between the topmost terminal on the stack and the next input symbol, SHIFT
- If the relation >. holds, REDUCE
- No relation, SYNTAX ERROR

This is the solution to the bottom up assignment!

\section*{Example}
\begin{tabular}{|l|l|l|l|}
\hline Handle/Output & Stack & Input & Reason \\
\hline & \$ & id + id *id \$ & Start State \\
\hline & \$ id & +id*id\$ & \$ <. id \\
\hline & & & \\
\hline & & & \\
\hline & & & \\
\hline & & & \\
\hline & & & \\
\hline & & & \\
\hline
\end{tabular}

\section*{Unary Operators}
- In your grammar: *, \& -
- Example: Unary prefix operator
\(\sim\) (not operator. Is not also a binary operator)
\(\mathrm{X}<. \sim\) for any op X
\(\sim>\). X if \(\sim\) has higher precedence than X , and \(\sim<\). X otherwise

\section*{Unary op is also a binary op}
- * is dereference and multiplication
- - is negation and subtraction
- \& is not also binary
- Use lexer to return different token for
- Dereference/Multiplication
- Negation/Subtraction
- How?
- Lexer needs to remember the previous token!
- Cannot look ahead

\section*{Define}
- Operator-precedence grammar is an \(\varepsilon\)-free operator grammar in which the precedence
relations <.,=.,>. constructed as previous are disjoint. For any pair of terminals, a and b, never more than one of the relations \(a<. b\), \(a=. b\), \(a>. b\) is true.

\section*{Create Table}
- Let G be an \(\varepsilon\)-free operator grammar
- For each two terminals a and b we say:
- \(\mathrm{a}=. \mathrm{b}\) if there exists a RHS: \(\alpha a \beta b \gamma\) where \(\beta\) is either \(\varepsilon\) or a single nonterminal.
- \(\mathrm{a}<. \mathrm{b}\) if for some NT A, a RHS \(\alpha \mathrm{a} A \beta\) exists, and \(A=>^{+} \gamma b \delta\), where \(\gamma\) is either \(\varepsilon\) or a single NT
- a >. b if for some NT A, a RHS \(\alpha \mathrm{Ab} \beta\) exists, and \(A=>^{+}\)pa \(\delta\), where \(\delta\) is either \(\varepsilon\) or a single NT

\section*{LEADING, TRAILING}
- LEADING: for each NT, those terminals that can be the first terminal in a string derived from that NT
- TRAILING: for each NT, those terminals that can be the last terminal in a string derived from that NT

\section*{Leading/Trailing}

\begin{tabular}{|c|c|c|}
\hline Nonterminal & First terminal & Last terminal \\
\hline E & & \\
\hline T & & \\
\hline F & & \\
\hline
\end{tabular}

\title{
Compute Precedence
}
- For =. look for RHS with two terminals separated by nothing or a NT
- <. Look for RHS with a terminal immediately to the left of a NT (a, A in rule above) For each, a is <. to any terminal LEADING(A)
- >. Look for a RHS with a nonterminal immediately to the left of a terminal (A, b rule above). Every terminal TRAILING(A) >. b

\section*{Compute Precedence}
- Algo 5.2 on handout!


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- EXTRA

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\section*{Create Operator Precedence Table}
- Page 207: heuristic for arithmetic expressions
- Precedence \& Associativity
- If op X has higher precedence than op Y , make \(\mathrm{X}>\). Y and \(\mathrm{Y}<. \mathrm{X}\)
- If op \(X\) and op \(Y\) have equal precedence, make \(\mathrm{X}>. \mathrm{Y}\) and \(\mathrm{Y}>. \mathrm{X}\) if they are left assoc. \(\mathrm{X}<. \mathrm{Y}\) and \(\mathrm{Y}<. \mathrm{X}\) if they are right assoc.
- \(\mathrm{X}<. \mathrm{id}\), id >. \(\mathrm{X}, \mathrm{X}<\). (, (<. X, ) >. \(\mathrm{X}, \mathrm{X}>\). ), X \(>\). \$, \$<.X, for all op X
- More on page 207

Build the table!
Operators Associativity
\begin{tabular}{lll|l} 
High & \(\wedge\) & right \\
& \(* /\) & left \\
\multirow{3}{*}{ Low } & +- & left
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline & \(+\) & - & * & / & \(\wedge\) & id & ( & ) & \$ \\
\hline \(+\) & & & & & & & & & \\
\hline - & & & & & & & & & \\
\hline * & & & & & & & & & \\
\hline / & & & & & & & & & \\
\hline \(\wedge\) & & & & & & & & & \\
\hline id & & & & & & & & & \\
\hline ( & & & & & & & & & \\
\hline ) & & & & & & & & & \\
\hline \$ & & & & & & & & & \\
\hline \multicolumn{10}{|c|}{CS 480 - Spring 2013} \\
\hline
\end{tabular}

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