## Database Topic Due Monday! (11:59pm)

- Brief paragraph explaining the topic, goals, and users of the database ( $1 / 2$ page at most)
- List of data (nouns) you will store
- does not need to be complete
- Three queries that your users will want to answer
- Worth 5 points (of 25 points for Design Documents)
- Submit electronically (GoogleDoc)
- CS445_DBTopic_PUNetID
- If I have any concerns, I'll ask you to schedule an appointment with me


# Normalization 

## Oct 5, 2009

## Chapter 19



## Problems

- Redundant Storage
- Update Anomalies
- Insertion Anomalies
- Deletion Anomolies


## Solutions

- Get rid of redundancy!
- Identify functional dependencies
- Decompose Relations
- Must preserve semantics of relations (don't lose data)
- and by lose we may mean gain
- Must preserve all dependencies (constraints)


## Function Dependency

- FD:
- Key
"If $X$-> $Y$ holds, where $Y$ is the set of all attributes, and there is no proper subset V of X such that V -> Y holds, then X is a key." ${ }^{1}$
- Superkey "If $X$-> $Y$ holds, where $Y$ is the set of all attributes, then $X$ is a superkey." ${ }^{1}$
- A key is also a superkey

¹http://www.imada.sdu.dk/~meer/dm26/

## Set of FDs

- Closure:
- $F$ is a set of $F D$ for Relation $R$, closure of $F$ is $F^{+}$
- Armstrong's Axioms:
- Reflexivity:
- Augmentation:
- Transitivity:
- Sound
- Complete


## Additional Rules

- Union:
- Decomposition:
- Trivial FD
- X -> Y: all attributes in Y are in X
- \{SID, Major, Name\} -> \{ Major, Name \}


## Normal Forms

- Boyce-Codd Normal Form (BCNF)
if there is an FD $B$->a in relation $R$ then
$B->a$ is trivial $(a \in B)$
or
$B$ is a superkey

From the Assignments:
FD \{ZoneName\} -> \{CommisionRate\}
Is Property in BCNF? Why or why not?

## $3^{\text {rd }}$ Normal Form

if there is an FD $B$->a in relation $R$ then
$B->a$ is trivial $(a \in B)$
or
$B$ is a superkey
or
a is part of some key for $R$

- Possible violations: X -> A

Less restrictive (weaker) than BCNF. More practical, easier to preserve dependencies.

- X is a proper subset of some key K
- partial dependency
- X is not a proper subset of any key
- transitive dependency
- Everything in BCNF is in 3NF, everything not in 3NF is not in BCNF


## Example 3NF

- BoatReservation (page 633 section 19.7.4)
(SailorID, BoatID, Date, CreditCard)
Key: (SailorID, BoatID, Date)
What type of relationship is this?
FD: \{SailorID\} -> \{CreditCard\}
What does this FD mean?

Is this in $3 N F ?$

Is this in BCNF?

## Example 3NF

- BoatReservation (page 619)
(SailorID, BoatID, Date, CreditCard)
Key: (SailorID, BoatID, Date)
FD: \{SailorID\} -> \{CreditCard\}

If we also have FD \{CreditCard\}->\{SailorID\} what does this FD mean?

Is this in $3 N F$ ?

Is this in BCNF?

## Decompositions

- To put a Relation R in BCNF:
- if $R$ is not in BCNF then there must be at least one nontrivial FD a -> B such that a is not a superkey for $R$.
- Rewrite R as two schemas:
- (a U B)
- ( $\mathrm{R}-(\mathrm{B}-\mathrm{a}))$


## Lossy Decomposition

| S | P | $D$ |
| :---: | :---: | :---: |
| s1 | p 1 | d 1 |
| s 2 | p 2 | d 2 |
| s 3 | p 1 | d 3 |

Original Relation

| S | P |
| :---: | :---: |
| s 1 | p 1 |
| s 2 | p 2 |
| s 3 | p 1 |


| $P$ | $D$ |
| :---: | :---: |
| $p 1$ | $d 1$ |
| $p 2$ | $d 2$ |
| $p 1$ | $d 3$ |

Decomposed Relations

What data was lost?
Test to determine losslessness:
When R is decomposed into R 1 and R 2 , the attributes common to R1 and R2 must contain a key for either R1 or R2.
Formally:
$\mathrm{F}^{+}$(of R) contains either FD R1 $\cap$ R2 -> R1 or FD R1 $\cap$ R2 ->R2

| s | p | d |
| :---: | :---: | :---: |
| s 1 | p 1 | d 1 |
| s 2 | p 2 | d 2 |
| s 3 | p 1 | d 3 |
| s 1 | p 1 | d 3 |
| s 3 | p 1 | d 1 |

New Relation

## Dependency Preservation

- "Allow us to enforce all FDs by examining a single relation instance" on each change of that relation instance
- Enforcing an FD across relations instances is expensive (if possible)
- If we decompose relation $R$ down in to $X$ and $Y$, the dependencies are preserved if $\left(F_{x} \cup F_{y}\right)^{+}=F^{+}$
- if we insert/delete/update into/from X or Y, we only need to examine the respective relation to check constraints


## Decomposition

- Relation (C,S,J,D,P,V,P)
- FD: \{C\}->\{C,S,J,D,P,V\}, \{J,P\} ->\{C\}, \{S,D\} -> \{P\} What FDs can we infer?

What are keys?

SuperKeys?

What violates BCNF?

How do we decompose this?
What dependency is not preserved?

Page 621 (with edits for clarity)

## Normalization

- The process of putting a schema in a particular normal form
- BCNF
- may not be a be able to create a dependency-preserving decomposition in BCNF
- 3NF
- can always create a lossless, dependency-preserving decomposition in 3NF


## Normalization to BCNF

- If $R$ is not in BCNF there must be at least one FD X->Y such that $Y$ is a single attribute and $X->Y$ violates $B C N F$.
- Decompose R into R-Y and XY
- Repeat while $R$ is not in BCNF
\{CSJDPQV\} FDs: \{JP\}->\{C\}; \{SD\}->\{P\}
- To preserve dependencies in BCNF, we may store some redundant information
- still can't always preserve dependencies, however \{CSP\} FDs: $\{C S\}->\{P\} ;\{P\}->\{C\} ;$ KEYs: $\{C S\},\{P S\}$


## Normalization to 3NF

- We can use the method above to get a lossless decomposition in BCNF (hence it is in 3NF)
- This does not ensure dependency preservation
- we need to add that for a 3NF normalization
- Minimal Cover set for FDs
- given a set of FDs F, a minimal cover set of FDs G is
- $X->A$ is in $G$, and $A$ is a single attribute
- $\mathrm{F}^{+}$is equal to $\mathrm{G}^{+}$
- if any FDs are deleted from G to form set $\mathrm{H}, \mathrm{H}^{+} \neq \mathrm{F}^{+}$


## Minimal Cover, example

- FDs $\{A\}->\{B\}\{A B C D\}->\{E\}\{E F\}->\{G\}\{E F\}->\{H\}\{A C D F\}-$ $>\{E G\}$
- Single attribute on Right:
- Minimize Left Side
- Remove redundant FDs


## Decomposition into 3NF

- $R$ is a relation with a set of FDs $F$ where $F$ is a minimal cover
- Produce a lossless decomposition as per BCNF
- produce relations $D=\left\{R_{1}, R_{2}, \ldots, R_{n}\right\}$
- Identify FDs in F not preserved in the closure of the FDs in $R_{1} \ldots R_{n}$
- for each non-preserved FD $\{X\}$->\{A\}, add relation XA to D

