### CS310

### Finite Automata Sections:

Sep 3, 2010

#### **Quick Review**

- Alphabet: ∑ = {a,b}
  - $\sum^*$ : Closure:
- String: any finite sequence of symbols from a given alphabet. |w| = length Concatenation/Prefix/Suffix/Reverse
- Language L over ∑ is a subset of ∑\*
  L= { x | rule about x}

Concatenation/Union/Kleene Star

**Recursive Definition** 

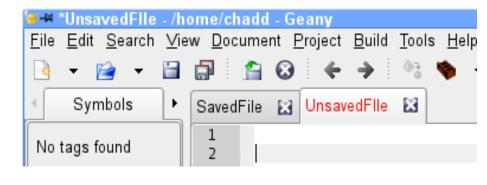
#### Finite Automata

• How can we reason about computation?

- Simple model of computation
  - Finite Automata
  - extremely limited amount of memory
  - represent states of computation

## Example

- File Editor (Geany)
  - saving mechanism
  - States?
  - Operations?

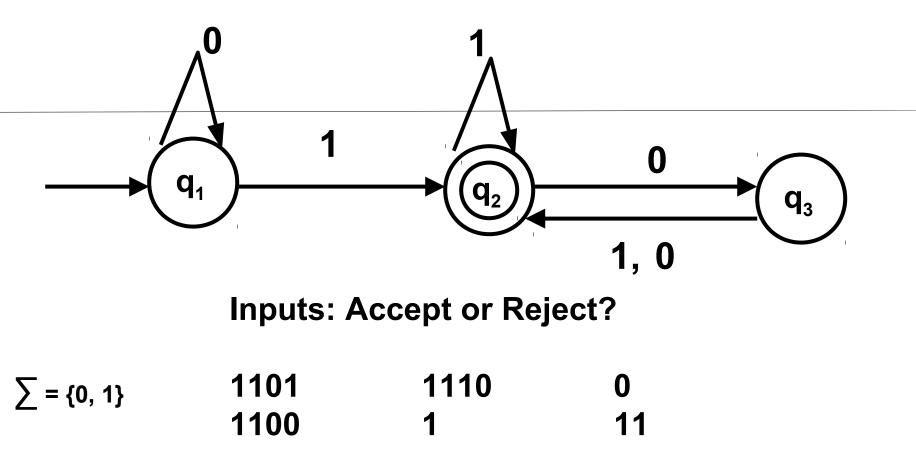


### Computation

- Recognize patterns in data
- Build an automata that can classify a string as part of a language or not
- Why?

Language: L = { x c {0,1}\* | x contains at least one 1 and the last 1 is followed by even number of 0s}

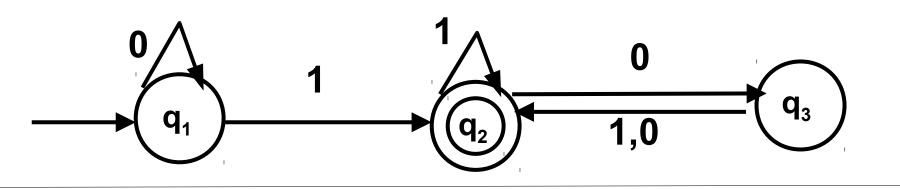
#### **Deterministic Finite Automata**



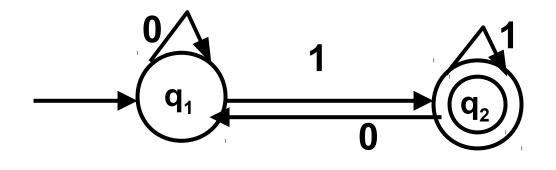
Set of all strings (A) accepted by a machine (M) is the *Language of the Machine* M *recognizes* A or M *accepts* A

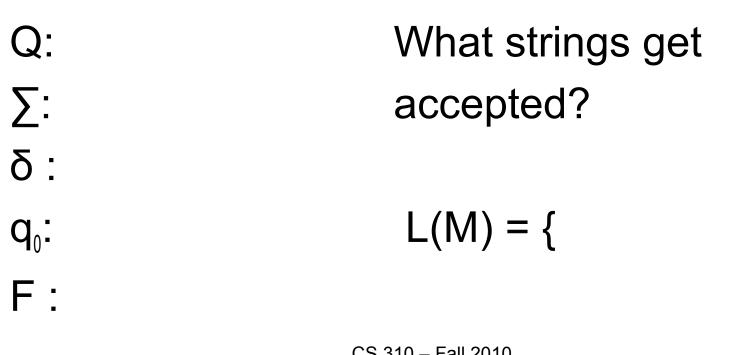
### **Formal Definition**

- Deterministic Finite Automata:
  - 5-tuple (Q,  $\sum$ ,  $\delta$ ,q<sub>0</sub>, F)
  - Q: finite set of states
  - $\Sigma$ : alphabet (finite set)
  - δ : transition function (δ: Qx∑−>Q)
  - q<sub>0</sub>: start state
  - F : accepting states (subset of Q)



- Q: finite set of states
- ∑: alphabet
- $\delta$  : transition function
- q<sub>0</sub>: start state
- F: accepting states





### Designing a DFA

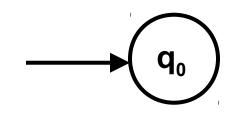
- Identify small pieces
  - alphabet, each state needs a transition for each symbol
  - finite memory, what crucial data does the machine look for?
  - can things get hopeless? do we need a trap?
  - where should the empty string be?
  - what is the transition into the accept state?
  - can you transition out of the accept state?
- Practice!

$$L(M) = \{ w | w = \varepsilon \text{ or } w \text{ ends in } 1 \}$$
  
 $\sum = \{ 0, 1 \}$ 

Q: δ: q<sub>0</sub>: F:

•  $\sum = \{0,1\}, L(M)=\{w \mid odd \# of 1s\}$ 

Build a DFA to do math! L(M) = Accept sums that are multiples of 3  $\sum = \{ 0,1,2, < Reset > \}$ Keep a running total of input, modulo 3



#### ∑ = {0,1}, L(M)={w | begins with 1, ends with 0}

#### • $\sum = \{0,1\}, L(M)=\{w \mid contains \ 110\}$

#### • $\sum = \{0,1\}, L(M)=\{w \mid does not contain 110\}$

•  $\sum = \{0,1\}, L(M)=\{w \mid (01)^*\}$ 

#### • $\sum = \{0,1\}, L(M)=\{w \mid w \text{ even } \#0s, \text{ odd } \#1s \}$

# ∑ = {0,1}, L(M)={w | w any string except 11 and 111 }

### Formal Definition of Computing

 Given a machine M= (Q, ∑, δ,q₀, F) and a string w=w₁w₂...w₀ over ∑, then M *accepts* w if there exists a sequence of states r₀,r₁...r₀ in Q such that:

$$-\mathbf{r}_0 = \mathbf{q}_{0:}\mathbf{r}_0$$
 is the start state

 $-\delta(r_i, w_{i+1}) = r_{i+1}, i=0,...,n-1$ : legal transitions

 $-r_n \in F$ : stop in an accept state

- M recognizes A if A={w | M accepts w}
- Language A is *regular* if there exists a Finite Automata that recognizes A.