

CS310

Nondeterministic Finite Automata

Sections: 1.2 page 47

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Nondeterminism

- What?
 - State diagram can have none, one, or many exiting arrows for each symbol at each state
 - ϵ -transition automatically taken without any input
- Why?
 - Recognizes same languages as DFA
(can convert NFA to DFA)
 - Often easier to build
 - Need machine that will run processes simultaneously

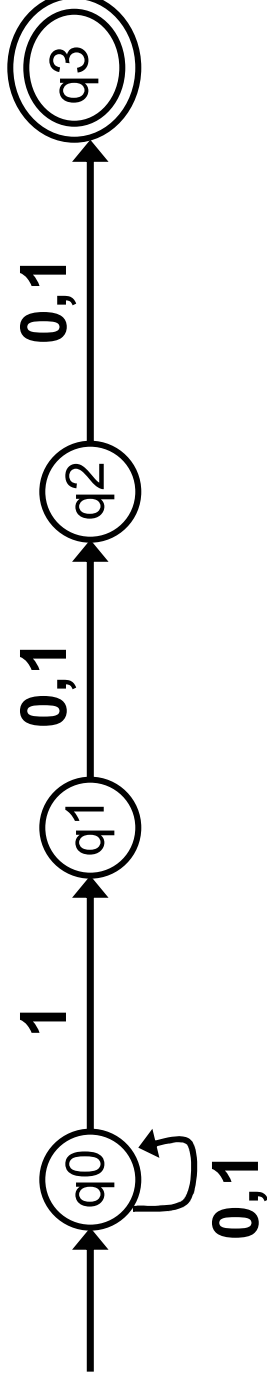
Example (1.30)

- Accept string of at least length three that contains a 1 in the third from end

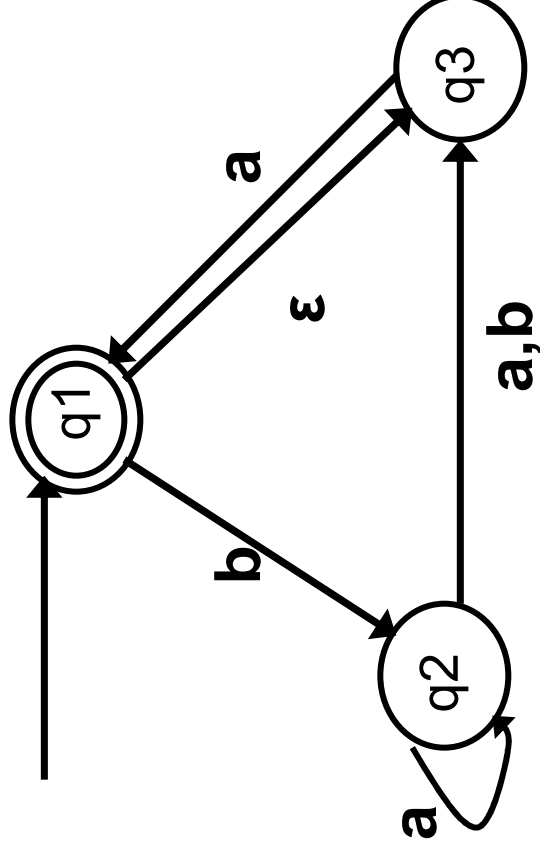
$$\Sigma = \{0,1\}, \quad \Sigma^*1(0U1)(0U1)$$

What makes this difficult for a DFA?

Equivalent DFA takes 8 states. Why 8?



Example



Accept: ϵ , a, baba, baa

Reject: b, bb, babba

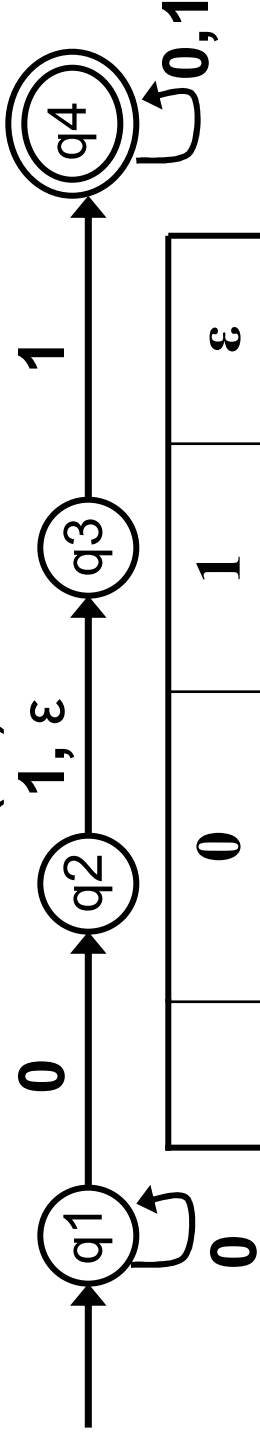
Formal Definition of NFA

- 5 tuple $(Q, \Sigma, \delta, q_0, F)$

$$\Sigma_\epsilon = \Sigma \cup \{\epsilon\}$$

$$\delta : Q \times \Sigma_\epsilon \rightarrow P(Q) \quad (\text{DFA: } \delta : Q \times \Sigma \rightarrow Q)$$

$P(Q)$ is the power set of Q . The collection of all subsets of Q . $P(Q)$ has $2^{|Q|}$ members



	0	1	ϵ
q1	{q1.q2}	\emptyset	\emptyset
q2	\emptyset	{q3}	{q3}
q3	\emptyset	{q4}	\emptyset
q4	{q4}	{q4}	\emptyset

Formal Definition of Computing for NFA

- Given a machine $M = (Q, \Sigma, \delta, q_0, F)$ and a string $w = w_1 w_2 \dots w_n$ over Σ , then M **accepts** w if there exists a sequence of states $r_0, r_1 \dots r_n$ in

Q such that:

- $r_0 = q_0$: r_0 is the start state
- $\delta(r_i, w_{i+1}) = r_{i+1}$, $i=0, \dots, n-1$: legal transitions
- $r_n \in F$: stop in an accept state

- Identical to the definition for the DFA!

Practice

- Construct a NFA with three states that recognizes $\{w \mid w \text{ ends with two } 0\text{s}\}$

$$\Sigma = \{0, 1\}$$

Practice

- Construct a NFA with six states
 $\{w \mid w \text{ even \# 0s OR exactly two 1s}\}$
 $\Sigma = \{0,1\}$

Practice

- Construct a NFA with three states

$0^*1^*0^*$

$\Sigma = \{0,1\}$