

# Trees

ZyBook: Chapter 6

(picture)

# Vocab

- root
- degree
- parent
- child
- leaf
- siblings
- ancestors

# Vocab

- descendants
- subtree
- level
- height of a tree
- depth of a node

# Binary Tree

- Any tree where a node has at most two children
- Very weak definition
- No one uses this

# Binary Search Tree

- Definition:
- Key / Value pair
- Why is this useful?

# Define a BSTNode

# Build a BST

- Key/Value: 201/Doug, 202/Chadd, 203/Shereen, 211/Chris
- What issues do we see?



# Walk the tree

- Pre order
- In order
- Post order

# bstSearch

# bstInsert

- Write an algorithm for bstInsert.
- What is the worst case computing complexity of your algorithm? Why?
- Write the C function bstInsert.



# FindLevel

- Write a C function `bstFindLevel` that returns the level of a node in a BST.



# Recursion!

- A function that calls itself!

```
int foo(int x)
{
    if( x > 0 )
    {
        return 2 + foo(x-1);
    }
    return 0;
}
```

```
foo(2); // ???
```

# Activation Records

- Each function adds one Activation Record
  - stack frame
- When the function terminates, the AR is popped off the stack



# Recursion!

- Draw the activation records for foo(2);

```
int foo(int x)
{
    if( x > 0 )
    {
        return 2 + foo(x-1);
    }
    return 0;
}
```

```
int main()
{
    foo(2); // ???
}
```

# Problem solving

- First step is to frame the problem in terms of itself.
  - a pattern
- Apply this pattern to create a recursive solution to the problem
- Divide a problem up into:
  - small unit of work
  - recursive call to do the rest of the work

# Example

- A factorial is defined as follows:

$$n! = n * (n-1) * (n-2) \dots * 1;$$

- For example:

$$1! = 1 \text{ (Base Case)}$$

$$2! = 2 * 1 = 2$$

$$3! = 3 * 2 * 1 = 6$$

$$4! = 4 * 3 * 2 * 1 = 24$$

$$5! = 5 * 4 * 3 * 2 * 1 = 120$$

Pattern? Small unit of work? Recursion?

# Problems

- Write `int factorial(int x)`
- `bstSearch()`
- `bstFindMaxDepth()`