## Integer Arithmetic

Reading: pp. 296-302

## Addition

In general, we know the following is true:

```
0 + 0 = 0 0
0 + 1 = 0 1
1 + 0 = 0 1
1+1=10
```

P1: Perform the following addition and interpret the result in: (a) modulo $2^{\wedge} \mathrm{n}$ and (b) two's complement notation.

```
010010101
10101010
```

$+000111001+10101010$

We must become familiar with the use of the carry. There are a couple of different carries that we must concern ourselves with. The carry-in and carry-out.

P2: Add the following two binary values discussing what is meant by carry-in and carryout.

```
    00001111
```

+01010101

Note: The carry-out of the MSB is the value that the external carry flag found in the flags register takes on.

Q1: In the previous example, what would be the value of the external carry? Why?

## Half-Adders and Adders

## Subtraction

Subtraction works a little differently than one would think. In particular, subtraction is performed by taking the two's complement of the subtrahend and adding this value to the minuend. Let's look at the following example for some clarification.

Perform the following subtraction:
00110011 (Minuend)
-00001111 (Subtahend)

Q2: Before performing the subtraction, identify the two numbers being subtracted. Assume the numbers are represented in modulo $2^{\wedge} \mathrm{n}$.

P3: Now perform the subtraction.
Q3: Interpret the result. Is it what you would expect it to be?
P4: Switch the minuend and the subtrahend from the above problems and then perform the subtraction. Interpret the result if the numbers are: (a) modulo $2^{\wedge} \mathrm{n}$ and (b) two's complement numbers.

## Arithmetic Overflow

Remember that the range of values that can be represented using 8 -bits for modulo $2^{\wedge} \mathrm{n}$ numbers is 0 to 255 and for two's complement is -128 to 127 . The microprocessor will perform the addition or subtraction of two numbers, but the question is how do we know if the result is correct. That is, if we add two 8 -bit numbers and the result is larger than the representation allows, how do we know this happened. The answer lies with two flags: (a) the carry flag and (b) the overflow flag.

First we will define overflow as a condition such that an arithmetic operation produces a result outside the range of the number system being used.

P5: Perform the operations below and interpret the result in: (a) modulo $2^{\wedge} n$ and (b) two's complement notation.

```
11111111 01111111
+00000001 +00000001
```

Q4: Were there any examples of overflow? Identify each case and briefly explain why.

Test each example using debug in Windows XP.



Let's perform the following additions and determine where any overflows occurred.

| 1001 | 1100 |
| ---: | ---: |
| +0101 | +0100 |
| -------- |  |
|  |  |
| 0011 | 1100 |
| +0100 | +1111 |
| ---- | ---- |
|  |  |
| 0101 | 1001 |
| +0100 | +1010 |
| ----- | ----- |

Let's perform the following subtractions and determine where any overflows occurred. Represent the numbers in 2's complement.
$2-7$
$5-2$
$(-5)-2$
$5-(-2)$
$7-(-7)$
$(-6)-4$

For each of the following, perform the additions, convert the binary numbers to decimal where the binary numbers are represented in two's complement, and indicate where a carry-out or overflow occurs.

| $\begin{array}{r} 11011001 \\ +01011100 \end{array}$ | $\begin{array}{r} 11101101 \\ +11111001 \end{array}$ | $\begin{array}{r} 00101100 \\ +00101101 \end{array}$ |
| :---: | :---: | :---: |
| $\begin{array}{r} 01101000 \\ +00101101 \end{array}$ | $\begin{array}{r} 10110101 \\ +00111011 \end{array}$ | $\begin{array}{r} 10011001 \\ +10111011 \end{array}$ |
| $\begin{array}{r} 00001010 \\ +11111101 \end{array}$ | $\begin{array}{r} 01111111 \\ +00000001 \end{array}$ | $\begin{array}{r} 11111111 \\ +00000001 \end{array}$ |

