# Algorithm Design and Analysis shereen@pacificu.edu CS380 Algorithm Design and Analysis What is an Algorithm? • A sequence of computational steps that transforms the *input* into the desired *output*. • To be interesting, an algorithm has to solve a general, specified problem. An algorithmic problem is specified be describing the set of instances that it must work on and the desired properties of the output. CS380 Algorithm Design and Analysis Do Algorithms Matter? • Once upon a time ... From Algorithms in a Nutshell. O'Reilly

### Do Algorithms Matter?

- Graham's Idea: write a program to find memory leaks
- Built a small library that wrapped the OS's memory allocation and deallocation routines with new functions.
- These functions recorded each allocation and deallocation in a data structure that would be queried at the end of the program

CS380 Algorithm Design and Analysis

## Do Algorithms Matter?

- Problem: Program ran really slowly
- · Gary to the rescue!

CS380 Algorithm Design and Analysis

### Do Algorithms Matter?

- Gary: Describe the problem and solution
- Graham: ....
- · Gary: Is there a difference in the performance of the programs?
- Graham: Small programs run in acceptable time, regardless if they had memory leaks. Programs that did a lot of processing and had memory leaks ran disproportionately

# Experiments: Program A int main(int argc, char \*\*argv) { for(int i = 0; i < 1000000; i++) { malloc(32); } exit(0); }</pre>

### Experiments: Program B

```
int main(int argc, char **argv)
{
  for(int i = 0; i < 1000000; i++)
  {
    void *x = malloc(32);
    free(x);
  }
  exit(0);
}</pre>
```

# Experiments: Program C

```
int main(int argc, char **argv)
{
  void *addrs[1000000];
  for(int i = 0; i < 1000000; i++)
  {
    addrs[i] = malloc(32);
  }
  for(int i = 0; i < 1000000; i++)
  {
    free(addrs[i]);
  }
  exit(0);
}</pre>
```

New Insight
It's not the number of memory allocations
open at the end of the program that affected
performance.
• Instead, it's
CS380 Algorithm Design and Analysis 10
Also with as a Mattaul
Algorithms Matter!
Gary: How do you track allocated memory?
Graham: A binary search tree. Each node is
a struct containing:
<ul><li>Pointers to children</li><li>Address of allocated memory</li></ul>
Size allocated
<ul> <li>Place in program where allocation was made</li> </ul>
<ul> <li>Memory address is the key for the nodes</li> </ul>
CS380 Algorithm Design and Analysis 11
Algorithms
Binary Search Tree is a good choice
Key is memory address
<ul> <li>malloc allocates memory from the heap in order of increasing memory address</li> </ul>
<ul> <li>What happens if addresses are 1-15 (for the sake of argument)?</li> </ul>
<ul> <li>What is the problem with Graham's code?</li> </ul>

Performance	
Algorithms is the study of computer-program performance	
What is more important than performance in computer programs?	
0	
0	
0	
0	
0	
CS380 Algorithm Design and Analysis 13	
	_
Why Study Algorithms?	
•	
•	
•	
•	
•	
•	
CS380 Algorithm Design and Analysis 14	
Compostoro	1
Correctness	
For any algorithm, we must prove that it	
always returns the desired output for all legal	
instances of the problem.	
<ul><li>What does this mean for sorting?</li></ul>	
	-
CS380 Algorithm Design and Analysis 15	

### Correctness is Not Obvious!

- · Suppose you have a robot arm equipped with a tool, say a soldering iron. To enable the robot arm to do a soldering job we must construct an ordering of the contact points so the robot visits (and solders) the first contact point, then visits the second point, third, and so forth until the job is done.
- Since robots are expensive, we need to find the order which minimizes the time (ie. travel distance) it takes to assemble the circuit board.

CS380 Algorithm Design and Analysis

### Correctness is Not Obvious!

 You are given the job to program the robot arm. Give me an algorithm to find the best

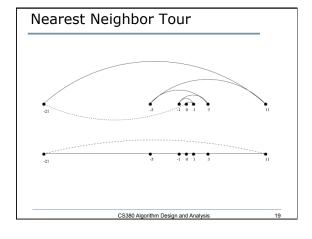


CS380 Algorithm Design and Analysis

### Nearest Neighbor Tour

- A very popular solution starts at some point  $p_0$  and then walks to its nearest neighbor p<sub>1</sub> first, then repeats from  $p_1$ , etc. until done.
- Pick and visit an initial point p<sub>0</sub>
- $p = p_0$
- i = 0
- · While there are still unvisited points
  - o i = i + 1
  - Let  $p_i$  be the closest unvisited point to  $p_{i-1}$
  - Visit p<sub>i</sub>
- Return to  $p_0$  from  $p_i$ CS380 Algorithm Design and Analysis

	·	



### Closest Pair Tour

 In this case we repeatedly connect the closest pair of points whose connection will not cause a cycle or a three-way branch to be formed, until we have a single chain with all the points in it.

Let n be the number of points in the set

d = ∞

For i = 1 to n-1 do

For each pair of endpoints (x, y) of partial paths It  $dist(x, y) \le d$  then  $x_m = x, y_m = y, d = dist(x, y)$ 

Connect  $(x_m, y_m)$  by an edge

Connect the two endpoints by an edge

CS380 Algorithm Design and Analysis

----

Closest Pair Tour
<ul> <li>So, is there a correct algorithm to solve this problem?</li> </ul>
CS380 Algorithm Design and Analysis 21

	=-
A Correct Algorithm	
	-
CS380 Algorithm Design and Analysis 22	
Why Not Use a Supercomputer	
A faster algorithm running on a slower	
computer will always win for sufficiently large	
instances	
Usually, problems don't have to get that large before the faster algorithm wins	
large before the faster argonithm wins	
CS380 Algorithm Design and Analysis 23	
	_
Expressing Algorithms	
What are the possible ways to express an	
algorithm?	
∘ English	
o Pseudocode	
Programming Language	
CS380 Algorithm Design and Analysis 24	

### The RAM Model

- Algorithms can be studied in a machine and language independent way.
- Each "simple" operation (+, -, =, if, call) takes exactly one step.
- Loops and subroutines are not simple operations.
- · Each memory access takes one step.

CS380 Algorithm Design and Analysis

25

### Best, Worst, and Average-Case

- Worst case: is the function defined by the maximum number of steps taken on any instance of size n.
- Best case: is the function defined by the minimum number of steps taken on any instance of size n.
- Average case: is the function defined by an average number of steps taken on any instance of size n.

CS380 Algorithm Design and Analysis

26

### Example: Sorting

- Input: A sequence of n numbers <a<sub>1</sub>, a<sub>2</sub>,
   ..., a<sub>n</sub>>
- Output: A permutation (reordering) <a  $_1$ , a  $_2$ , ..., a  $_n$ > of the input sequence such that a  $_1$   $\le$  a  $_2$   $\le$  ...  $\le$  a  $_n$
- We seek algorithms that are *correct* and *efficient*

CS380 Algorithm Design and Analysis

27

### **Insertion Sort**

- INSERTION-SORT(A,n)  $\nabla$  A[1..n]
- 1 **for** j ← 2 **to** n
- 2 **do** *key* ← A[j]
- 3  $\nabla$  Insert A[j]
- 4 i ← j 1
- while i > 0 and A[i] > key
- 6 **do** A[i+1] ← A[i]
- 7 i ← i 1
- 8  $A[i+1] \leftarrow key$

CS380 Algorithm Design and Analysis

# Example

- How would insertion sort work on the following numbers?
  - 03 1 7 4 8 2 6

CS380 Algorithm Design and Analysis

### Your Turn

- Problem: How would insertion sort work on the following characters to sort them alphabetically (from A -> Z)? Show each step.
  - oS OR TED

Insertion Sort			
Is the algorithm correct?			
<ul><li>How efficient is the algorithm?</li></ul>			
<ul> <li>How does insertion sort do on sorted permutations?</li> </ul>			
<ul> <li>How about unsorted permutations?</li> </ul>			
CS380 Algorithm Design and Analysis 3'	 31		
Analysis of Insortion Sort			
Analysis of Insertion Sort			
Best Case			
CS380 Algorithm Design and Analysis 33	32		
Analysis of Insertion Sort			
Worst Case			
CS380 Algorithm Design and Analysis 33	33		

For Next Time
Read Chapters 1 and 2 from the book.