



Math122 College Algebra

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2.4

Lines

- The slope of a line is $slope = \frac{rise}{run}$
- For a line in the coordinate plane
 - run is the change in the x-coordinate
 - rise is the change in the y-coordinate

Slope of a Line

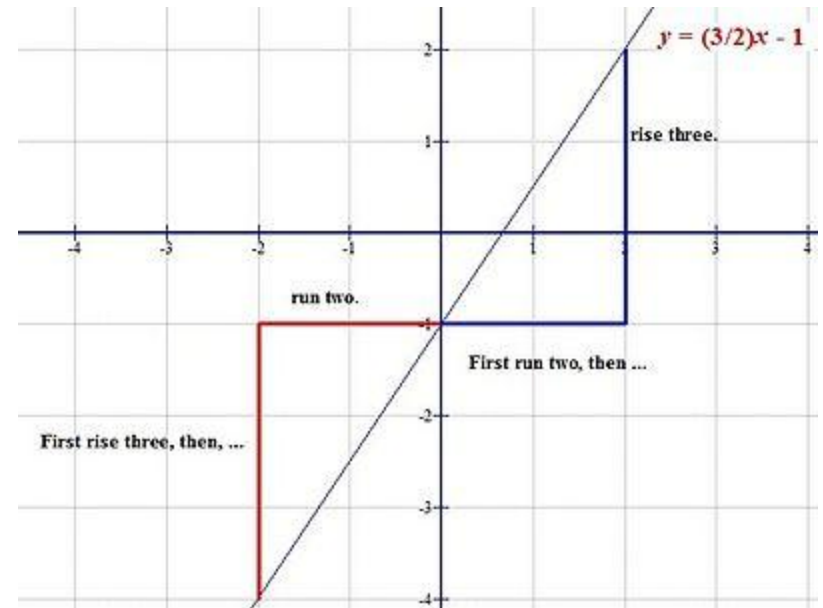
- The slope m of a nonvertical line that passes through points $A(x_1, y_1)$ and $B(x_2, y_2)$ is

$$m = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1}$$

- The slope of a vertical line is undefined. Why?

Slope of a Line

- The slope is independent of which two points are chosen on the line
- Compute the slope using two different sets of points



<http://en.wikipedia.org/wiki/Slope>

Problem

1. Find the slope of the line that passes through the points $P(2,2)$ and $Q(4,5)$.
2. Using the slope find two more points that lie on the same line defined in 1.

Point-Slope Form

- An equation of the line passing through the point $P(x_1, y_1)$ with slope m is

$$y - y_1 = m(x - x_1)$$

- Find an equation of the line through $(1, -3)$ with slope $\frac{1}{2}$. Sketch the line
- Find an equation of the line through $(1, -3)$ with slope $-\frac{1}{2}$

Problem

1. Find an equation of the line passing through the two points $(1,1)$ and $(3,4)$. Sketch the line.
2. Find an equation of the line passing through the two points $(-3, -2)$ and $(3, -6)$. Sketch the line.

Slope-Intercept Form

- An equation of the line with slope m and y – *intercept* is $y = mx + b$
- Find the equation of the line with slope 2 and y -intercept -1
- Find the slope and y -intercept of the line $2x + y = -5$