

# Math122 College Algebra

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### Ch1.1 Equations

- Equations are a mathematical tool for solving problems in the real-world
- An equation such as 2 + 4 = 6 states that two mathematical expressions are equal
- Equations of interest contain variables such as 3x + 2 = 11
- *x* is an unknown in the above equation
- solutions (or roots) are values that make the equation true
- solving an equation is the process of finding the solutions of the equation

# Equations

- Equivalent equations are two equations with the same solutions
- Solving an equation is the process of finding equivalent equations where the variable is isolated on one side of the equal sign
- Solve 3x + 2 = 11Answer  $3x + 2 = 11 \iff 3x = 9 \iff x = 3$
- $\Leftrightarrow$  means equivalent to

#### **Properties of Equality**

- 1.  $A = B \iff A + C = B + C$  means we can produce an equivalent equation by adding the same value to both sides of an equation
- 2.  $A = B \iff AC = BC \ (C \neq 0)$  means we can produce an equivalent equation by multiplying the same non-zero value to both sides of an equation

# Linear Equations

- A linear equation in one variable is of the form ax + b = 0 where
  - *1. a* and *b* are real numbers
  - *2.* x is the variable

• Place an L by a linear equation and a N by a nonlinear equation for each equation below

1. 
$$2x + 3 = 0$$

2.  $y^2 + y = 1$ 3.  $2a = \frac{1}{2}a + 5$ 

4. 
$$\frac{-}{x} = 1$$
  
5.  $\sqrt{y} - 2y = 0$ 

• Solve the following equations for *x* and check your results.

1. 
$$4x - 3 = 2x - 6$$

2. 
$$\frac{-2x}{3} = -12$$

3. 
$$\frac{5x-20}{3x} = \frac{5}{9}$$

## Equation with no Solution

• Solve the following equation for y and check your results.

1. 
$$2 + \frac{5}{x-4} = \frac{x+1}{x-4}$$

# **Solving Power Equations**

Linear equations have variables only to the first power

• What about equations that involve squares, cubes, ...

• Example  $2y^2 - 4 = 0$ 

### **Solving Power Equations**

• The power equation  $X^n = a$  has the solution  $X = \sqrt[n]{a}$  if n is odd  $X = \pm \sqrt[n]{a}$  if n is even and  $a \ge 0$ 

 Note: If n is even and a < 0, the equation has no real roots

• Solve each of the following equations. 1.  $y^3 = 27$ 

#### 2. $a^2 = 4$

#### *3.* $x^2 = -4$

• Solve each of the following equations and check your answer.

1. 
$$y^2 - 3 = 0$$

2. 
$$(y-3)^2 = 3$$

*3.* 
$$(y+3)^2 = -3$$

Solve each of the following equations and check your answer.

*1.* 
$$y^3 = -27$$

2. 
$$16a^4 = 81$$

3. Solve 
$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$
 for  $R_1$