

STACK ADT

Stack

- The stack is a LIFO (Last-in First-out) linear data structure.
- The only data element that can be removed is the most recently added element.

Stack ADT Specification

- Elements: Stack elements can be of any type, but we will assume StackElement.
- **Structure**: Any mechanism for determining the elements order of arrival into the stack.

- **Domain**: The number of stack elements is bounded. A stack is considered full if the upper-bound is reached. A stack with no elements is considered empty.
- **Operations**: There are seven operations as follows:

function create (s: Stack, isCreated: boolean) **results**: if s cannot be created, isCreated is false; otherwise, isCreated is true, the stack is created and is empty

function terminate (s: Stack) results: stack s no longer exists

function isFull (s: Stack) **results**: returns true if the stack is full; otherwise false is returned

function isEmpty (s: Stack) **results**: returns true if the stack is empty; otherwise, false is returned

function push (s: Stack, e: StackElement) **requires**: isFull (s) is false **results**: element e is added to the stack as the most recent element

function pop (s: Stack, e: StackElement) **requires**: isEmpty(s) is false **results**: The most recently added element is removed and assigned to e

function peek (s: Stack, e: StackElement) requires: isEmpty(s) is false results: The most recently added element is assigned to e but not removed

Testing your Data Structure

- Your customer will abuse your data structure
- Your data structure should never crash the customer's code
 - code defensively
- Test each each function
 - test each function's requires statement
 - test boundary conditions (full/empty)
 - test bad input
 - test functions called in the wrong order

What are Stacks Useful for?

- Web browser history.
- "undo" in applications.
- Runtime stack.

Ex. 2: Balancing Parentheses

- Parentheses in algebraic expressions need to be balanced in order for the expression to be correct.
- Which of the following are valid expressions?
 - {a^2 [(c d)^2 + (e f)^2] }
 - {a [(b + c))) (d + e)] }
 - {a [[[(b + c) (d + e)] }
 - {a [(b + c) (d + e) }]
- How can a stack be used to test if an expression's parentheses are balanced?