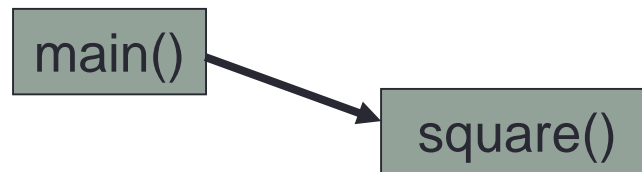


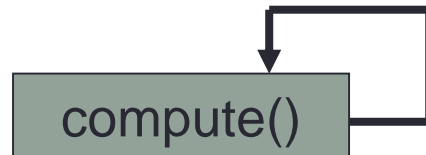
RECURSION

Recursive Functions

- All function calls that we have seen so far have been made by other functions



- A recursive function is a function that calls itself



Recursion

- Some problems are more easily solved using recursion
- Tree functionality is more easily solved by recursion than by iteration

First Recursive Problem

```
void count (int index)
{
    printf ("%d", index);
    if (index < 2)
    {
        count (index + 1);
    }
}

int main ()
{
    count (0);
    return 0;
}
```

What is the output?

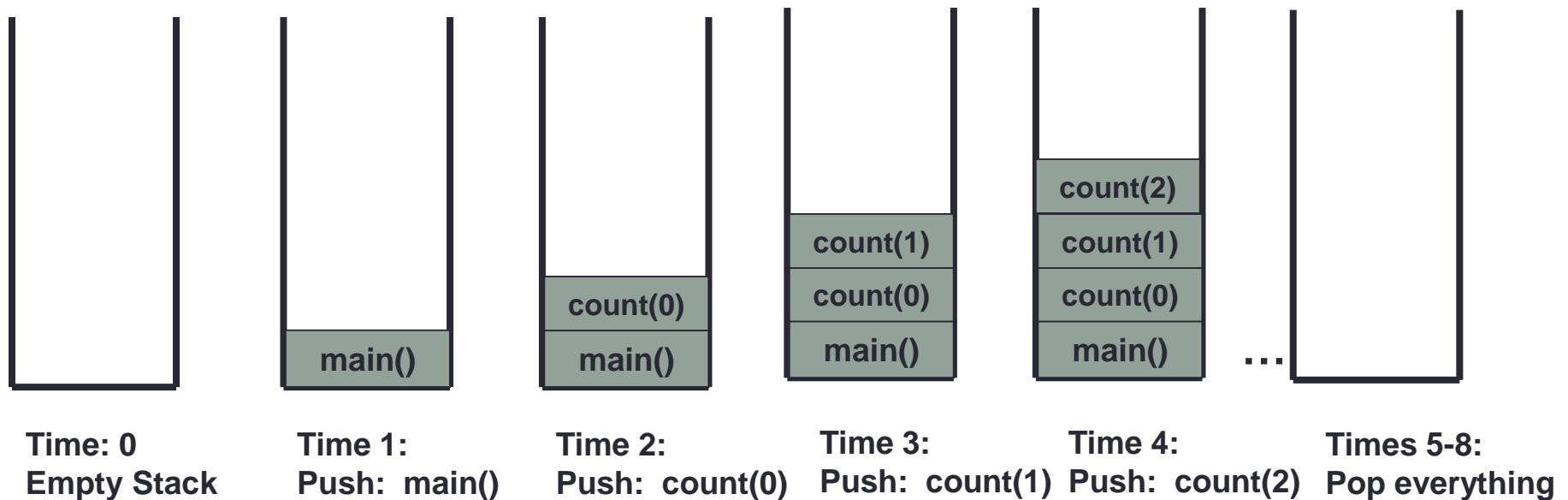
Visualizing Recursion

- To understand how recursion works, it helps to visualize what is going on
- We will do this using *Activation Records (stack frames)* and the *Call Stack (runtime stack)*
- Each time a function is called, an activation record is created and pushed on to the top of the stack
- When the function returns, the activation record is popped off the stack

Recursion and the Call Stack

- When a method calls itself recursively, you just push another copy of the function on to the top of the stack

Recursion and Call Stacks



Yes, printf () generates an AR each time count () is called

What is the Output?

```
void count (int index)
{
    printf ("%d", index);
    if (index < 2)
    {
        count (index + 1);
    }
}
```

```
int main ()
{
    count (3);
    return 0;
}
```


Recursion and Factorials

- Computing factorials are a classic problem for examining recursion.

- A factorial is defined as follows:

$$n! = n * (n-1) * (n-2) \dots * 1;$$

- For example:

$$1! = 1 \text{ (Base Case)}$$

$$2! = 2 * 1 = 2$$

$$3! = 3 * 2 * 1 = 6$$

$$4! = 4 * 3 * 2 * 1 = 24$$

$$5! = 5 * 4 * 3 * 2 * 1 = 120$$

Recursion and Factorials

- First step is to frame the problem in terms of itself. You do this by finding a pattern
- Once you see the pattern, you can apply this pattern to create a recursive solution to the problem
- Divide a problem up into:
 - What it can do (usually a base case)
 - What it cannot do
 - What it cannot do resembles original problem
 - The function launches a new copy of itself (recursion step) to solve what it cannot do

Recursive Factorial Solution

```
int main ()
{
    int i;

    for (i = 1; i <= 10; ++i)
    {
        printf ("%d!: %d\n", i, factorial (i));
    }
    return 0;
}
```