

Proof:

(PDA)  $P = (Q, \Sigma, \Gamma, \delta, q_0, \{q_{\text{accept}}\})$

Convert PDA to CFG

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Variables of  $G$  (grammar) are:  $\{A_{pq} \mid p, q \text{ is in } Q\}$

Start variable is  $A_{q_0, q_{\text{accept}}}$

$G$ 's rules:

For each  $p, q, r, s$  in  $Q$ ,  $t$  in  $\Gamma$ , and  $a, b$  in  $\Sigma$ ,

if  $\delta(p, a, \varepsilon)$  contains  $(r, t)$  and  $\delta(s, b, t)$  contains  $(q, \varepsilon)$  then  
ADD RULE:  $A_{pq} \rightarrow aA_{rs}b$

For each  $p, q, r$  in  $Q$

ADD RULE:  $A_{pq} \rightarrow A_{pr}A_{rq}$

For each  $p$  in  $Q$

ADD RULE:  $A_{pp} \rightarrow \varepsilon$