

CS310

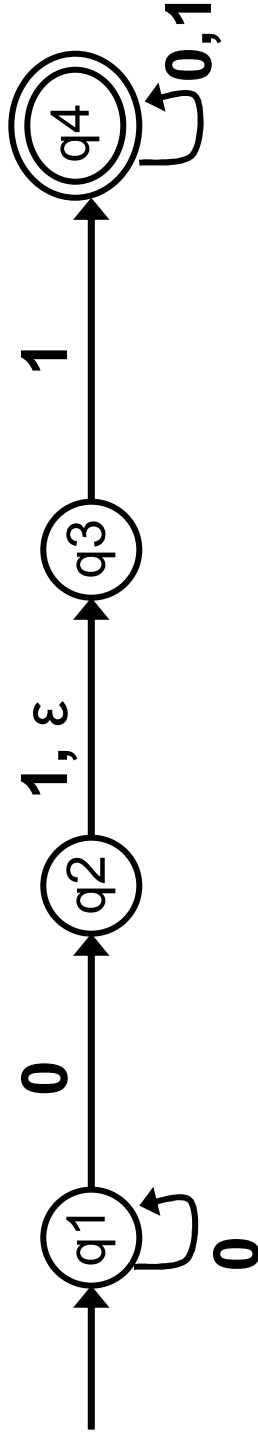
Converting NFA to DFA

Sections: 1.2 Page 54

September 13, 2006

Quick Review

- 5 tuple $(Q, \Sigma, \delta, q_0, F)$
 $\Sigma_\epsilon = \Sigma \cup \{\epsilon\}$
 $\delta : Q \times \Sigma_\epsilon \rightarrow P(Q)$ (DFA: $\delta : Q \times \Sigma \rightarrow Q$)
 $P(Q)$ is the power set of Q .



Convert NFA to DFA

- Two machines are equivalent if they recognize the same language
- Every NFA has an equivalent DFA (Th 1.39)
- $\delta_{\text{nfa}} : Q \times \Sigma_{\epsilon} \rightarrow P(Q)$
- The DFA will need to represent all subsets in $P(Q)$ (how many?)
 - let's assume no ϵ -transitions initially

Convert NFA to DFA

- NFA is $N = (Q, \Sigma, \delta, q_0, F)$
- DFA is $M = (Q', \Sigma', \delta', q_0', F')$

$$Q' = P(Q)$$

$$q_0' = \{q_0\}$$

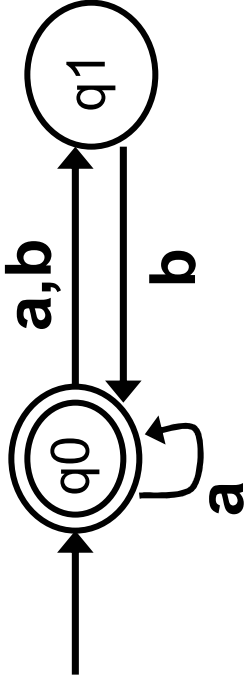
$$F' = \{R \in Q' \mid R \text{ contains an accept state of NFA}\}$$

$$\delta': Q' \times \Sigma' \rightarrow Q'$$

$$(P(Q) \times \Sigma \rightarrow Q)$$

Example (without δ)

NFA



$Q = \{q_0, q_1\}$

$\Sigma = \{a, b\}$

$Q_0 = q_0$

$F = \{q_0\}$

δ	a	b
q_0	$\{q_0, q_1\}$	$\{q_1\}$
q_1	$\emptyset$	$\{q_0\}$

DFA

$Q' = \{\emptyset,$

$\Sigma' = \{a, b\}$

$Q'_0 =$

$F' = \{$

Let's define the δ'

$\delta : Q \times \Sigma \rightarrow P(Q)$ in NFA

$\delta' : Q' \times \Sigma \rightarrow Q'$ in DFA

$R \in Q'$, $a \in \Sigma$

$\delta'(R, a) = \{ q \in Q \mid q \in \delta(r, a) \text{ some } r \in R \}$

Union of all sets that can be reached from a state
in set R using the δ with input a

$\delta'(R, a) = \bigcup_{r \in R} \delta(r, a)$

Converting NFA to DFA - ϵ Transitions

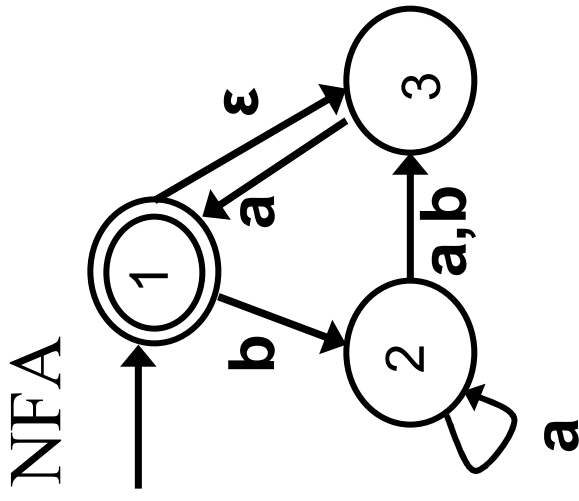
- Define start state and δ' to include all states that can be reached from a given state by 0 or more ϵ transitions

$E(R) = \{ q \mid q \text{ can be reached from } R \text{ by using } 0 \text{ or more } \epsilon \text{ transitions} \}$

$\delta'(R, a) = \{ q \in Q \mid q \in E(\delta(r, a)) \text{ for some } r \in R \}$

$\delta'(R, a) = \{ q \in Q \mid q \in \delta(r, a) \text{ some } r \in R \}$

Conversion Example (with δ)



$$Q = \{1, 2, 3\}$$

$$\Sigma = \{a, b\}$$

$$Q_0 = 1$$

$$F = \{1\}$$

DFA

$$Q' = \{\emptyset,$$

$$\Sigma' = \{a, b\}$$

$$Q'_0 =$$

$$F' = \{$$